

State University of New York

EECE 301 Signals & Systems Prof. Mark Fowler

<u>Note Set #22</u>

- D-T Signals: Frequency-Domain Analysis
- Reading Assignment: Section 4.1 of Kamen and Heck

Course Flow Diagram

The arrows here show conceptual flow between ideas. Note the parallel structure between the pink blocks (C-T Freq. Analysis) and the blue blocks (D-T Freq. Analysis).



Ch. 4: Fourier Analysis of D-T Signals

In this chapter we do for D-T signals what we did for C-T signals in Ch. 3:

– Define a D-T FT (DTFT) for D-T signals and see that it works pretty much like the FT for C-T signals (CTFT)

But... we also do something we can't do for CTFT-based ideas:

– Develop a <u>computer-processing version</u> of the DTFT... called the Discrete Fourier Transform (DFT) that will allow you to use the computer to numerically compute a "view" of the DTFT

Order of Coverage:

- <u>Sect. 4.1</u>: DTFT & It's Properties
- Sect. 4.2 & 4.3: The DFT & DFT-Based Signal Analysis
- Note: Section 4.4 is NOT covered

– Sect. 4.5 provides some applications of DFT analysis... we'll cover some other applications in class

4.1 Discrete-Time FT (DTFT)

Recall: Sampling Analysis



But we "did" this using a FT of a signal inside the DAC... Is there some other way to do this by <u>using the *samples*</u>?

Motivation for D-T Fourier Transform (DTFT)







Re-Define to Get The DTFT! $\left|\widetilde{X}(\omega) = \sum_{n=1}^{\infty} x[n] e^{-jn\omega T}\right|$ $n = -\infty$ Let $\Omega = \omega T$ where $T = 1/F_s$ **DTFT:** $X(\Omega) = \sum_{n=1}^{\infty} x[n]e^{-jn\Omega}$ $n = -\infty$

Ω is called "D-T Frequency"

 $\Omega = \omega T$: (rad/sec) × (sec/sample) = rad/sample

 $X(\omega)$ and $X(\Omega)$ are really the same thing...

just "plotted" w.r.t. a different unit

ω: rad/secΩ: rad/sample





Motivating D-T System Analysis using DTFT

