

State University of New York

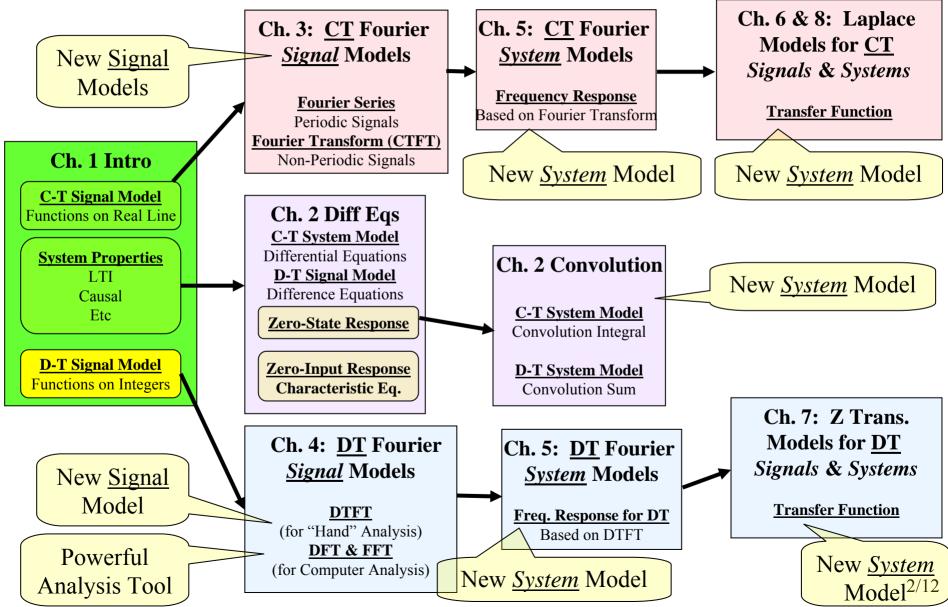
# EECE 301 Signals & Systems Prof. Mark Fowler

# Note Set #3

- What are Discrete-Time Signals???
- Reading Assignment: Section 1.2 of Kamen and Heck

## **Course Flow Diagram**

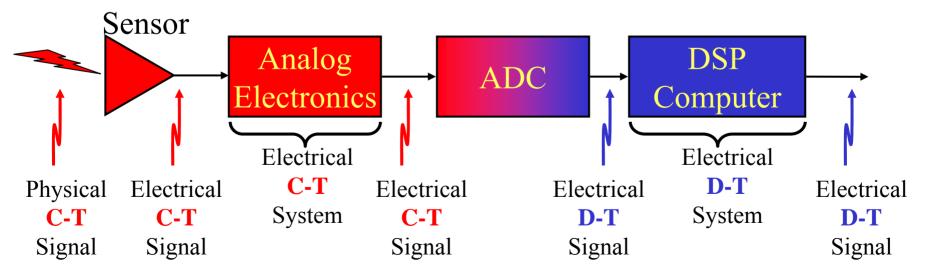
The arrows here show conceptual flow between ideas. Note the parallel structure between the pink blocks (C-T Freq. Analysis) and the blue blocks (D-T Freq. Analysis).



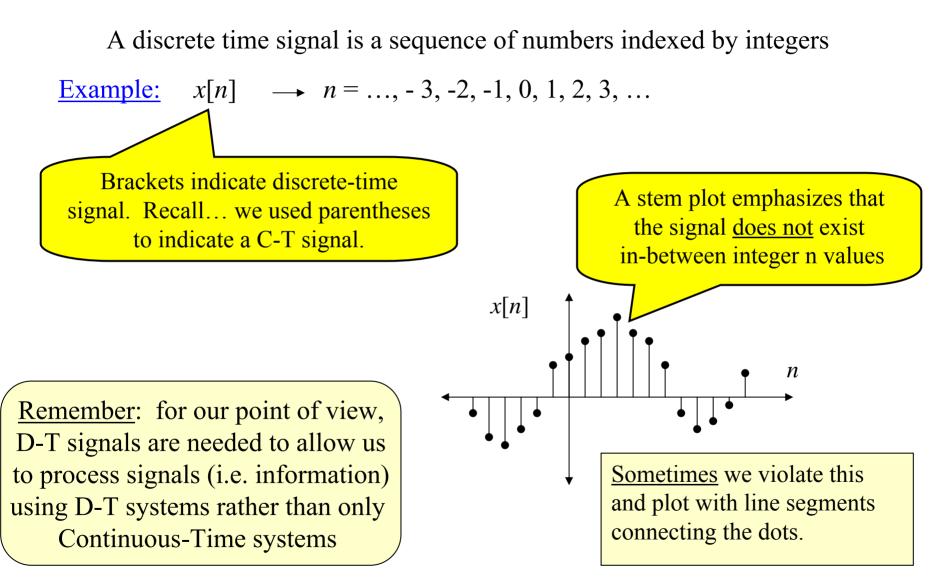
# **1.2 Discrete-Time (D-T) Signals**

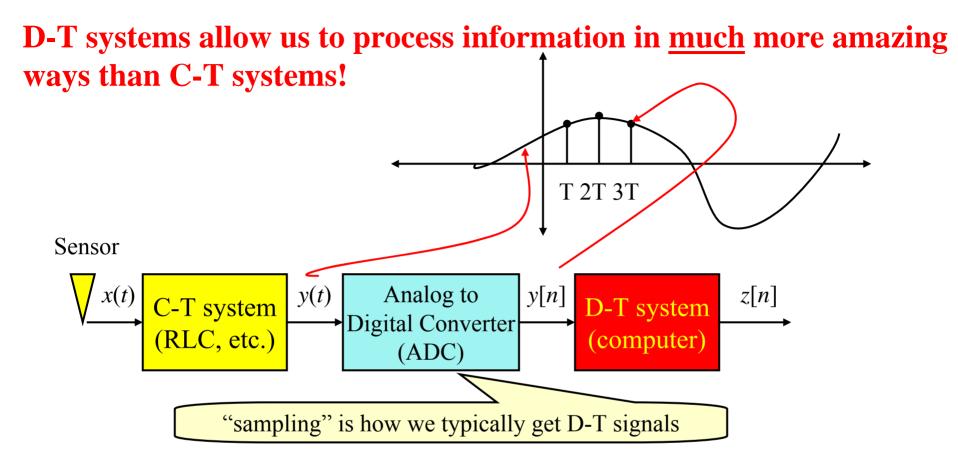
Recall from Note Set #1 that a common scenario in today's electronic systems is to do most of the processing of a signal using a computer.

A computer can't directly process a C-T signal but instead needs a stream of numbers... which is a **<u>D-T signal</u>**.



## What is a discrete-time (D-T) signal?





In this case the D-T signal *y*[*n*] is related to the C-T signal *y*(*t*) by:

$$y[n] = y(t)|_{t=nT} = y(nT)$$

T = time spacing between samples (seconds) $1/T = \text{sampling rate } (F_s) \text{ in samples/second}$ 

*T* is "sampling interval"

*F*<sub>c</sub> is "sampling rate"

**<u>Ex</u>**: CD audio is sampled at 44,100 samples per second  $\Rightarrow T = 1/44,100 \cong 22.68 \ \mu sec$ 

**Major Question**: How fast should we sample a specific signal?

(We can't answer that until Chapter 5!!)

Hint: You may know that humans can't hear frequencies above approximately 20kHz. Therefore, audio signals typically are limited to have no frequencies above 20kHz. Note that CD audio uses a sampling rate that is slightly more than twice this "highest" frequency!!

## **Digital Signals**

-A practical ADC not only gives a D-T signal but also one that is "digital" Can take values only from a finite set Don't confuse "digital" with logic signals!!! -An ADC represents each sample y[n] using a finite number of bits (typically 8 to 16 bits/sample)

-ADC's have a min/max input voltage

-If the ADC uses *B* bits per sample and V = max = - min volts Then there are  $2^B$  levels or values that are spaced  $\frac{2V}{2^B} = V2^{(-B+1)}$  volts apart

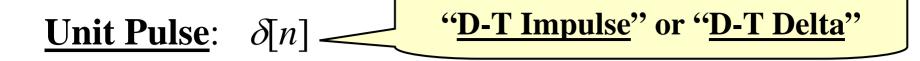
This "quantization" of values causes degradation in the quality of the representation of y[n]

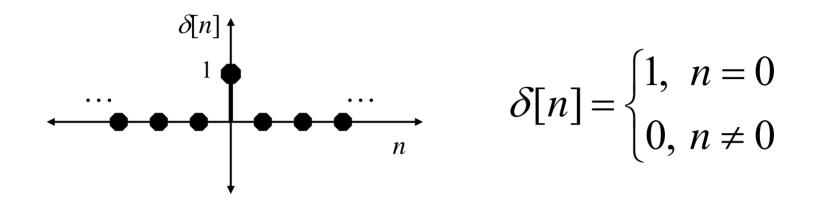
**For this course** we will ignore the quantization! **Our D-T signals can take on any value!**  Much of what we learned about C-T signals carries over to D-T signals

The **<u>D-T Unit Step</u>** is defined in an obviously similar way that the C-T Unit Step was defined. The D-T unit step is just a sampled version of the C-T unit step

The same holds true for the **D-T Unit Ramp.** 

However... there are a Few Exceptions...

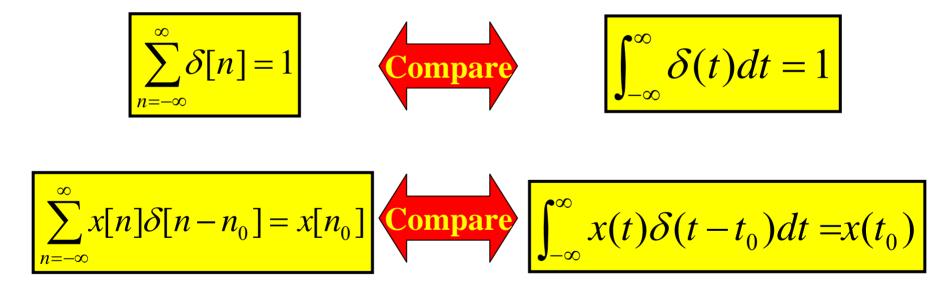




<u>Note:</u>  $\delta[n]$  is <u>not</u> a sampled version of  $\delta[t]$ 

#### **Sifting Property for D-T Delta Function**

Note: $\delta[n]$  works inside summations the same way $\delta(t)$  works inside integrals

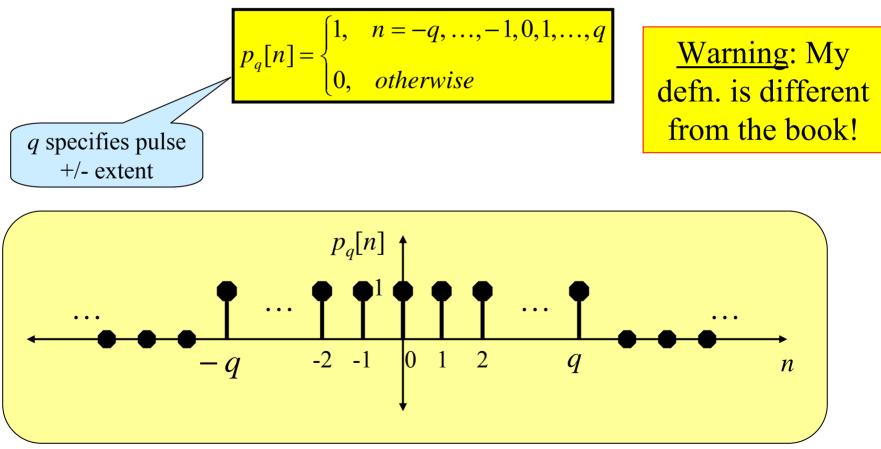


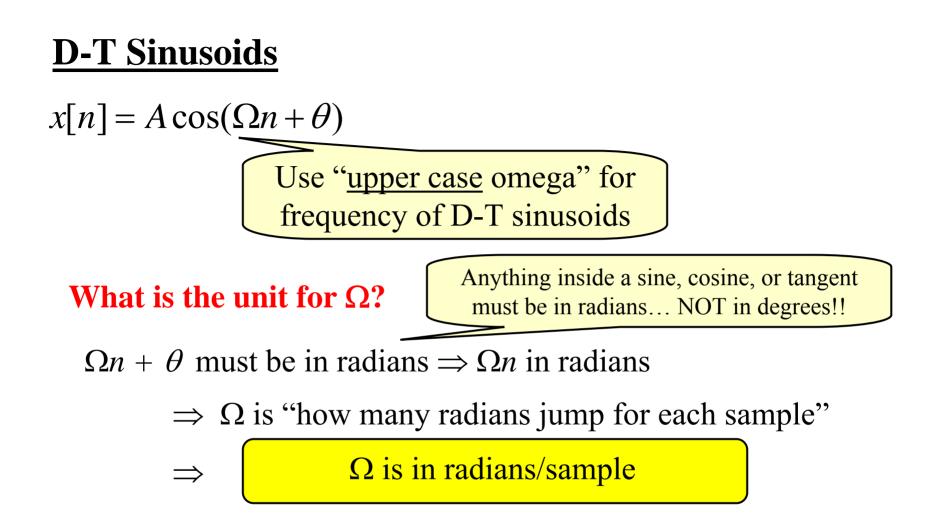
### **D-T Rectangular Pulse**

Often in practice we need to use pulses to model real-world signals...

One definition of DT version of this is as follows.

Let q be an integer, then a centered pulse of 2q+1 samples is





Other than the above difference... D-T sinusoids are pretty much like C-T sinusoids.