

## Fourier Transform Table

Time Signal	Fourier Transform
$1, -\infty < t < \infty$	$2\pi\delta(\omega)$
$-0.5 + u(t)$	$1/j\omega$
$u(t)$	$\pi\delta(\omega) + 1/j\omega$
$\delta(t)$	$1, -\infty < \omega < \infty$
$\delta(t-c), c \text{ real}$	$e^{-j\omega c}, c \text{ real}$
$e^{-bt}u(t), b > 0$	$\frac{1}{j\omega + b}, b > 0$
$e^{j\omega_0 t}, \omega_0 \text{ real}$	$2\pi\delta(\omega - \omega_0), \omega_0 \text{ real}$
$p_\tau(t)$	$\tau \text{sinc}[\tau\omega/2\pi]$
$\tau \text{sinc}[\tau t/2\pi]$	$2\pi p_\tau(\omega)$
$\left[1 - \frac{2 t }{\tau}\right] p_\tau(t)$	$\frac{\tau}{2} \text{sinc}^2[\tau\omega/4\pi]$
$\frac{\tau}{2} \text{sinc}^2[\tau t/4\pi]$	$2\pi \left[1 - \frac{2 \omega }{\tau}\right] p_\tau(\omega)$
$\cos(\omega_0 t)$	$\pi[\delta(\omega + \omega_0) + \delta(\omega - \omega_0)]$
$\cos(\omega_0 t + \theta)$	$\pi[e^{-j\theta}\delta(\omega + \omega_0) + e^{j\theta}\delta(\omega - \omega_0)]$
$\sin(\omega_0 t)$	$j\pi[\delta(\omega + \omega_0) - \delta(\omega - \omega_0)]$
$\sin(\omega_0 t + \theta)$	$j\pi[e^{-j\theta}\delta(\omega + \omega_0) - e^{j\theta}\delta(\omega - \omega_0)]$

## Fourier Transform Properties

Property Name	Property	
Linearity	$ax(t) + bv(t)$	$aX(\omega) + bV(\omega)$
Time Shift	$x(t - c)$	$e^{-j\omega c} X(\omega)$
Time Scaling	$x(at), \quad a \neq 0$	$\frac{1}{ a } X(\omega/a), \quad a \neq 0$
Time Reversal	$x(-t)$	$X(-\omega)$ $\overline{X(\omega)}$ if $x(t)$ is real
Multiply by $t^n$	$t^n x(t), \quad n = 1, 2, 3, \dots$	$j^n \frac{d^n}{d\omega^n} X(\omega), \quad n = 1, 2, 3, \dots$
Multiply by Complex Exponential	$e^{j\omega_0 t} x(t), \quad \omega_0 \text{ real}$	$X(\omega - \omega_0), \quad \omega_0 \text{ real}$
Multiply by Sine	$\sin(\omega_0 t)x(t)$	$\frac{j}{2} [X(\omega + \omega_0) - X(\omega - \omega_0)]$
Multiply by Cosine	$\cos(\omega_0 t)x(t)$	$\frac{1}{2} [X(\omega + \omega_0) + X(\omega - \omega_0)]$
Time Differentiation	$\frac{d^n}{dt^n} x(t), \quad n = 1, 2, 3, \dots$	$(j\omega)^n X(\omega), \quad n = 1, 2, 3, \dots$
Time Integration	$\int_{-\infty}^t x(\lambda) d\lambda$	$\frac{1}{j\omega} X(\omega) + \pi X(0)\delta(\omega)$
Convolution in Time	$x(t) * h(t)$	$X(\omega)H(\omega)$
Multiplication in Time	$x(t)w(t)$	$\frac{1}{2\pi} X(\omega) * W(\omega)$
Parseval's Theorem (General)	$\int_{-\infty}^{\infty} x(t)\overline{v(t)} dt = \frac{1}{2\pi} \int_{-\infty}^{\infty} X(\omega)\overline{V(\omega)} d\omega$	
Parseval's Theorem (Energy)	$\int_{-\infty}^{\infty} x^2(t) dt = \frac{1}{2\pi} \int_{-\infty}^{\infty}  X(\omega) ^2 d\omega \quad \text{if } x(t) \text{ is real}$ $\int_{-\infty}^{\infty}  x(t) ^2 dt = \frac{1}{2\pi} \int_{-\infty}^{\infty}  X(\omega) ^2 d\omega$	
Duality: If $x(t) \leftrightarrow X(\omega)$	$X(t)$	$2\pi x(-\omega)$